

## Lecture 11 - Oct. 20

### Syntactic Analysis

***CFG: Formulation***

***From RE or DFA to CFG***

***Ambiguity, Dangling else***

## Announcements

- **Programming Test**
  - + 2:00pm to 3:20pm on Saturday, October 29
  - + Venue to be confirmed (LAS building)
- **Project** teammates (gather at the end of the class)

# CFG: Formal Definition

Design the CFG for strings of properly-nested parentheses.

e.g., ( ), ( ) ( ), ( ( ( ) ( ) ) ) ( ), etc.

Present your answer in a formal manner.

$$S \rightarrow (S) \mid SS \mid \epsilon$$

N.T.  
T.

A **context-free grammar (CFG)** is a 4-tuple  $(V, \Sigma, R, S)$ :

- $V$  is a finite set of **variables** / non-terminals
- $\Sigma$  is a finite set of **terminals**.
- $R$  is a finite set of **rules** s.t.

$$R \subseteq \{V \rightarrow s \mid v \in V \wedge s \in (V \cup \Sigma)^*\}$$

$$s \in V^x \quad s \in \Sigma^x \quad [V \cap \Sigma = \emptyset]$$

$$(V \cup \Sigma)^*$$

$$s \in V^* \vee s \in \Sigma^*$$

- $S \in V$  is the **start variable**.

Rules.

$$\begin{aligned} S &\rightarrow (S) \\ S &\rightarrow SS \end{aligned}$$

mix of t. and n.t.  
variables

Given strings  $u, v, w \in (V \cup \Sigma)^*$ , variable  $A \in V$ , a rule  $A \rightarrow w$ :

$uAv \Rightarrow uwv$  means that  $uAv$  **yields**  $uwv$ .

$u \Rightarrow^* v$  means that  $u$  **derives**  $v$ , if:

- $u = v$ ; or
- $u \Rightarrow u_1 \Rightarrow u_2 \Rightarrow \dots \Rightarrow u_k \Rightarrow v$

[ a **yield sequence** ]

Given a CFG  $G = (V, \Sigma, R, S)$ , the language of  $G$

$$L(G) = \{w \in \Sigma^* \mid S \Rightarrow^* w\}$$

no non-terminals.

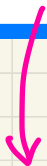
# Context-Free Grammar (CFG): Example Version 3

<b>Expr</b>	→	Expr + Term
		Term
<b>Term</b>	→	<u>Term * Factor</u>
		Factor
<b>Factor</b>	→	(Expr)
		a

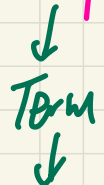
Example:  $a * a + a$

↳ Exercise: draw PT.

different precedences.



Expr → Expr + Term



Term \* Factor

higher precedence

# Context-Free Grammar (CFG): from RE (1)

RE	CFG
$L(\underline{\epsilon})$	$S \rightarrow \epsilon$
$L(\underline{a})$ $a \in \Sigma$	$S \rightarrow a$
$L(\underline{E} \oplus \underline{F})$	$S \rightarrow \text{cfg}(E) \mid \text{cfg}(F)$
$L(\underline{EF})$	$S \rightarrow \text{cfg}(E) \text{cfg}(F)$
$L(\underline{E}^*)$	$S \rightarrow \epsilon \mid S \text{cfg}(E)$
$L(\underline{(E)})$	$S \rightarrow (\text{cfg}(E))$

## Context-Free Grammar (CFG): from RE (2)

$(0 + 1)^* 1 (0 + 1)^*$

$(00 + 1)^* + (11 + 0)^*$

$S \rightarrow TUV$

$T \rightarrow \varepsilon \mid TT_2$

$T_2 \rightarrow 0 \mid 1$

$U \rightarrow 1$

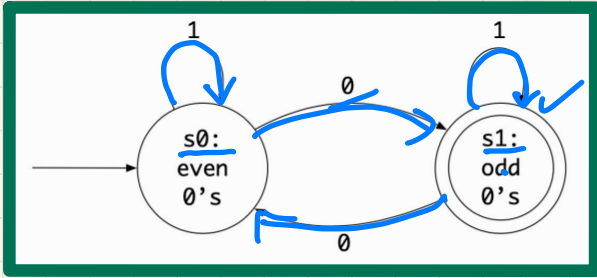
$V \rightarrow 0 \mid 1$

CFG

$\downarrow$   
Chomsky  
Normal  
Form

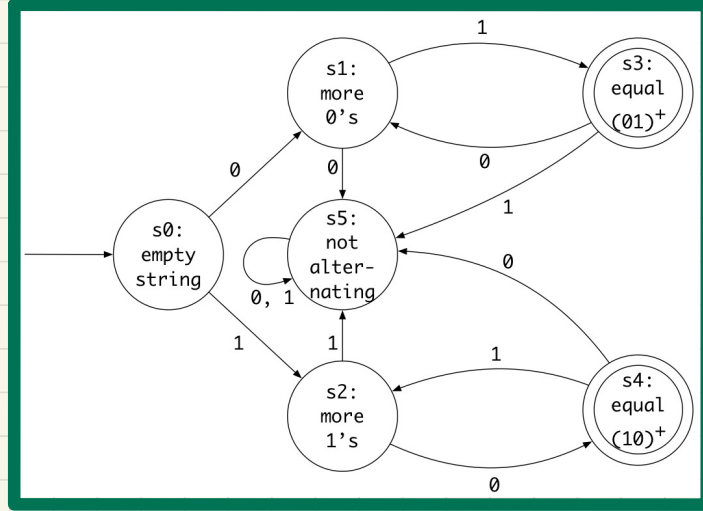
Exercise

# Context-Free Grammar (CFG): from DFA



$$S_0 \rightarrow 0S_0 \mid 1S_1$$

$$S_1 \rightarrow \epsilon \mid 1S_1 \mid 0S_0$$



Exercise